The Foundation Program, Deanship of General Studies, cordially invites you to attend:

# FP Virtual Academic Excellence Days Spring 2020

11 - 14 May 2020

# Teaching Math Beyond the Facts

BY: DR. DIANA REYOS – MALABANAN FOUNDATION PROGRAM, DEPARTMENT OF MATHEMATICS Trying to teach in the 21<sup>st</sup> century without conceptual schema for knowledge is like trying to build a house without a blueprint.

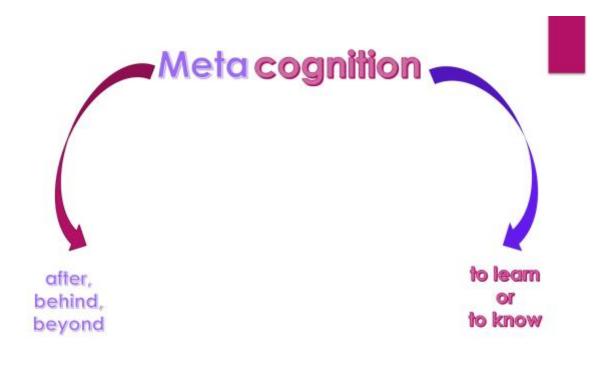
> -H. Lynn Erickson Concept-Based Curriculum and Instruction

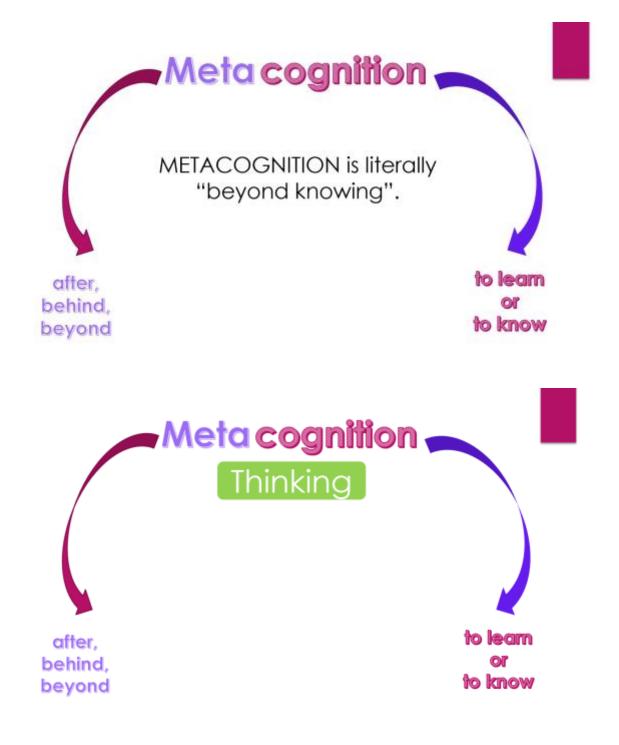
### Introduction

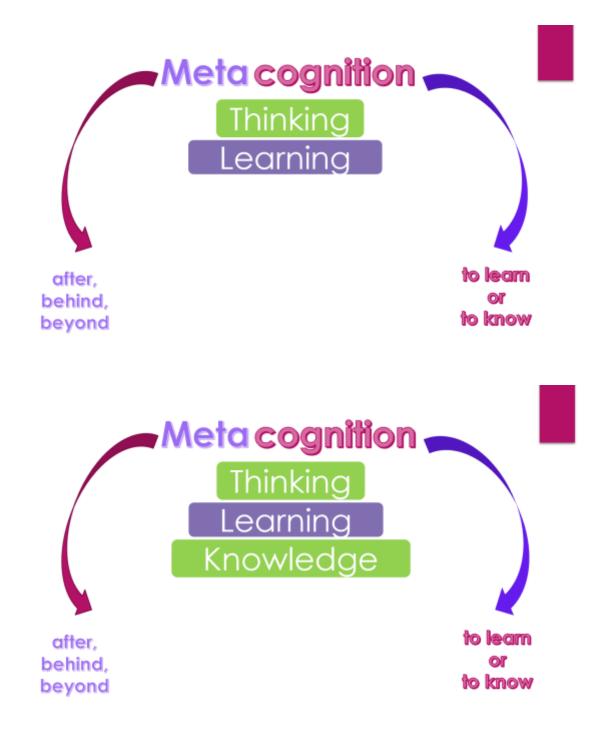


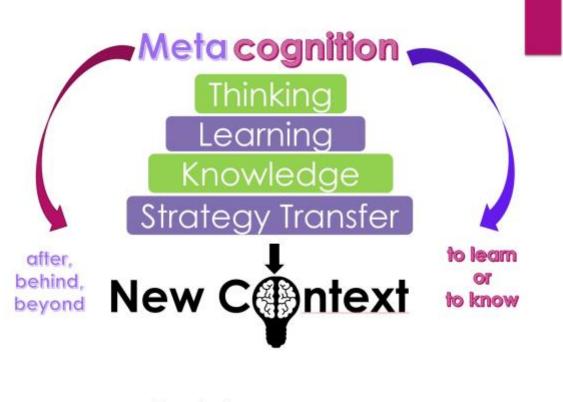
## METACOGNITION

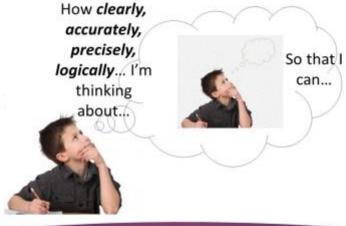
John Flavell, a psychologist of Stanford University is regarded as a foundation researcher in metacognition. Metacognition was first coined by Flavell In the mid 1970s. The term Metacognition as used by Flavell (1979) refers to an individual's awareness of his/her cognitive processes and strategies.



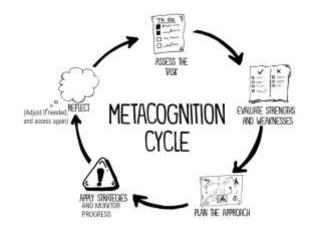




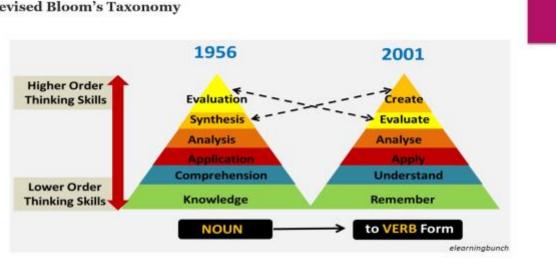




What are you thinking?



### Revised Bloom's Taxonomy and Research Studies



#### Revised Bloom's Taxonomy

Revised Bloom's Taxonomy uses verbs to describe the levels of thinking

- swaps the order of evaluate and create to represent objectives addressing synthesis/creation as a highest type.
- Emphasis is placed upon its use as more authentic tool for curriculum planning, instructional delivery, and assessment.

#### Metacognition in Revised Bloom's Taxonomy



 Krathwohl and Anderson revised the version of Bloom's Taxonomy to represent the 21<sup>st</sup> Century learners.

#### **Cognitive Complexity** Evaluate oduce new or original work Create n, assemble, construct, conjecture, develop, rate, author, investigate Create Justify a stand or decision Approved, angue, defend, judge, select, support, white onlique, wrigh Evaluate thesh lie Draw connections among ideas Merenciate, organize, relate, compo samine, experiment, question, test Analyze Keowledg Use information in new situations Decute, implement, solve, use, demonstrate, interp operate, schedule, sketch Apply dedar Explain ideas or concepts Inter Andge efficiency of Design Offician Understand Darsify describe discuss explain, identify locate, recognize, report, select, translate Recall facts and basic concepts Define, duplicate, list, memoriae, repeat, state Rollington Remember

## **Research Studies - metacognition**

#### Suriyon, et. al., (2013)Students' Metacognitive Strategies in the Mathematics Classroom Using Open Approach

#### Research results illustrate the importance of metacognitive strategies, which could bring about successful student mathematical problem solving. It could be seen that students could solve problems successfully; they tried to find various problem-solving strategies and could continue solving problems without giving up their efforts to create new problem solving approaches and to express various ways of thinking by using problem solving tools of previously learned ideas and strategies.

#### Kwon, et al. (2010) Students' Retention of Mathematical Knowledge and Skills in Differential Equations

This study investigates students' retention of mathematical knowledge and skills in two differential equations classes. Posttests and delayed posttests after 1 year were administered to students in inquiry-oriented and traditional classes. The results show that students in the inquiry-oriented class retained conceptual knowledge, as seen by their performance on modeling problems, and retained equal proficiency in procedural problems, when compared with students in the traditionally taught classes. The results of this study add additional support to the claim that teaching for conceptual understanding can lead to longer retention of mathematical knowledge. Friedlander, Alex; Arcavi, Abraham (2012) Practicing Algebraic Skills: A Conceptual Approach problem-based

Learning rules and procedures should be linked to a deeper understanding of their meaning and to a flexible choice of solution methods (Kieran 2004; star 2007; NCTM 2000). The authors write for mathematics teachers who wish to add a conceptual dimension to the practice of algebraic procedures. They describe an approach in which rules, procedures, algorithms, sense making, meaningful reading, and the creation of algebraic expressions are thoroughly integrated into the learning process. These practice-oriented activities require the adoption of some additional higherorder thinking skills, such as developing alternative solutions, evaluating the effectiveness of approaches, participating in class discussions, and reflecting on learned procedures and solution methods.

Aydina, Y. (2014) The effects of problem-based approach on student's conceptual understanding in a university mathematics classroom

The activities provided intensive treatment of a particular concept through student discovery and also gave students problem solving experience. The collaborative aspects of PBLA meet this challenge as students are provided a more customized teaching of calculus through personal interactions with group members and the instructor. **Project Based Learning activities with metacognitive regulations is an effective means for teaching mathematical concepts** which students generally enjoy working on the real. world problems. PBLA with collaborative groups can help students to achieve to learn the function concept better than the traditional teaching method and make a successful transition to university mathematics study .

## **Research Studies - metacognition**

#### Higher Order Thinking (HOT) - involves Metacognition

- HOT does not include memorization.
- HOT requires that we do something beyond the facts.



# What am I learning?

# How am I learning?



We all think...but are we using HOT skills?

## Enrich Math Questions



## Instead of

Solve:  $16(4 - 3m) = 96\left(-\frac{m}{2} + 1\right)$ 

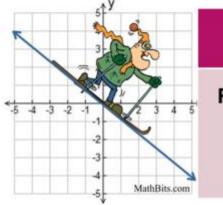
Find p in the equation -px + 1 =13 - 4(x + 3).

Solve: 2x + 7 = 2(x + 5)

Find the slope of the line passing

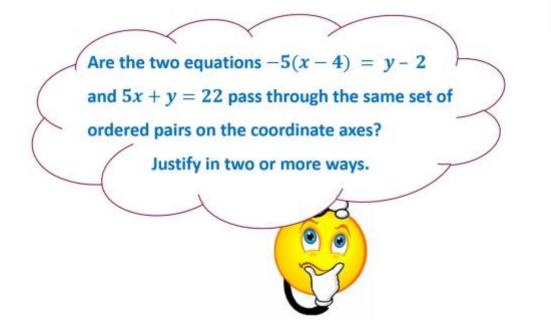
## Consider asking...

Determine whether the equation 16(4 - 3m) = $96\left(-\frac{m}{2}+1
ight)$  is an identity. Explain your answer. a. The equation -px + 1 = 13 - 4(x + 3) is an identity if p = \_\_\_. b. Find the value of p in the equation -px + 1 =13 - 4(x + 3), when x is 2. True of False: The equation 2x + 7 = 2(x + 5) has one solution. Justify your answer. If the slope of the line passing through (x, 17) and through points (1, 17) and (5, -3). (5, -3) is -5, then what is x?



## Instead of

Find the slope of the line passing through points (1, 17) and (5, -3).



## Hey, students!

# Go to student.desmos.com and type in:



You can also share this link with your students:

https://student.desmos.com/?prepopulateCode=g3nkb6



The area of the table is given in polynomial form  $x^2 + 12x + 36$ . Find an expression that represents dimension of the table. What is its shape? Explain your answer.

# Instead of

## Is the relation

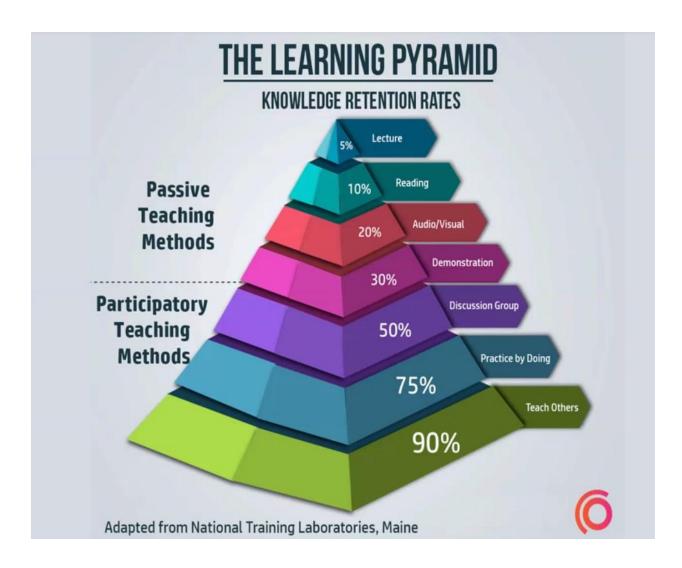
## $R = \{(4,3), (4,2), (1,6), (-4,0)\}$

## a function or not?



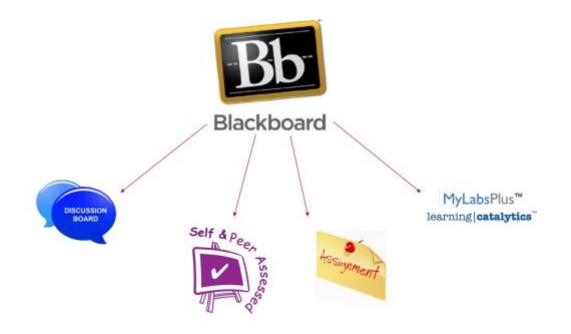
### **Assessment Methods and Tools**

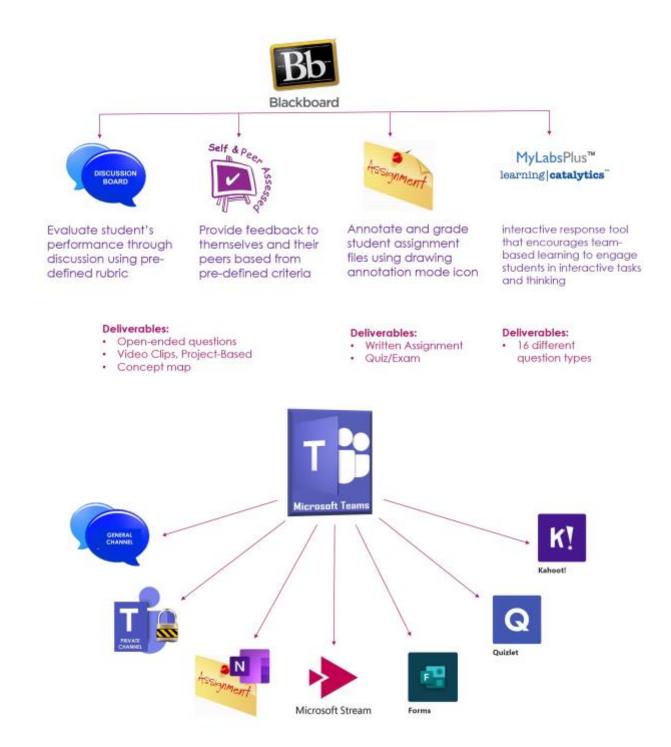


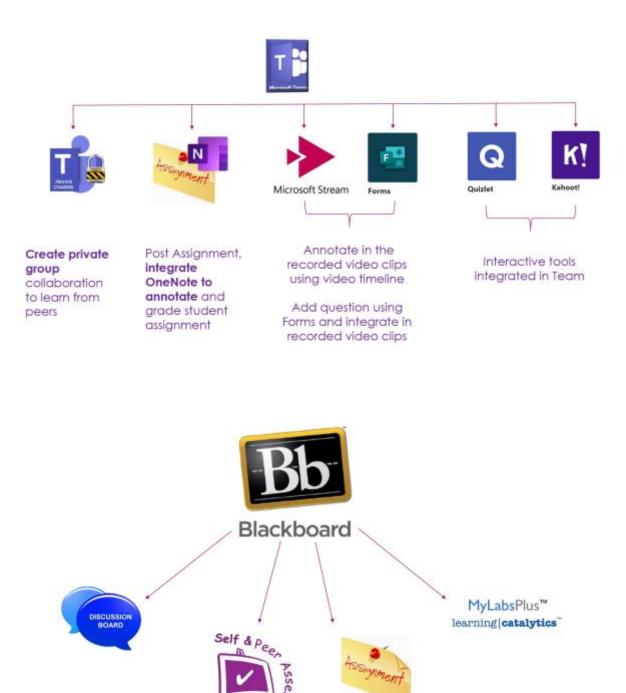














Evaluate student's performance through discussion using pre-defined rubric

**Deliver** Individually or by Group

#### **Deliverables:**

- Conceptest Open-ended
- questions .
- Video Clips
- Project-Based
- Concept map

#### **Grading Forum Participation**

You can assign discussion grades to evaluate participants on performance throughout a forum. Only users with the role of manager or grader can assign grades for posts. Graders can't view their own work.

I

- 1. In the forum where you enabled grading, select Grade Discussion Forum.
- 2. On the Grade Discussion Forum Users page, select Grade in a student's row. The student's posts are counted in the Posts column.

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#### Self and Peer Assessment: Submission and Evaluation Settings

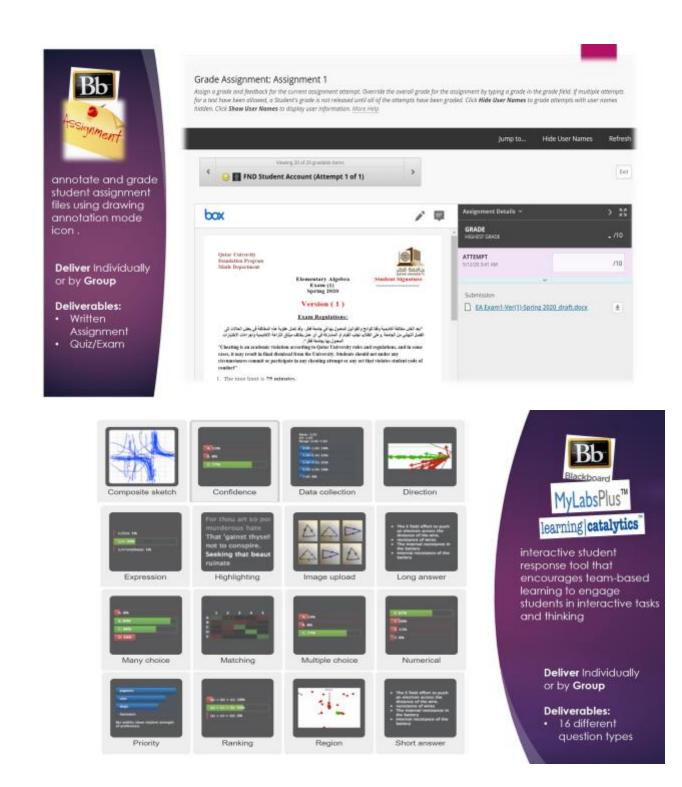
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Provide feedback to themselves and their peers based from predefined criteria

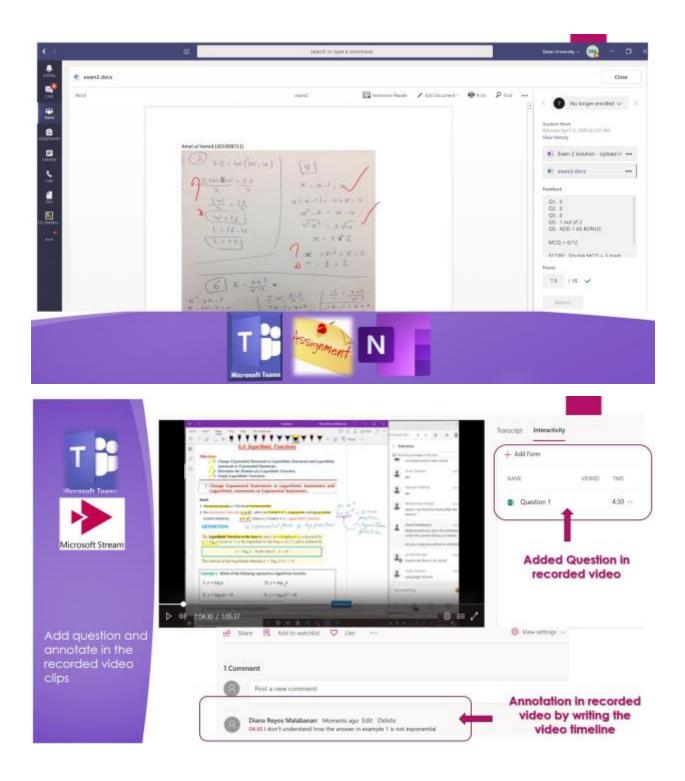


Conceptest

- Open-ended questions
- Video Clips Project-Based Concept map









# **Other Tools**



Group Member Evaluation The tool streamlines how students assess their peers' collaboration skills. The teacher specifies the criteria students use to evaluate their peers' contribution to group work.



Interactive Study Material



Interactive Presentation

method. Teachers can share media sources (audio, document, video) for students to discuss, answer practice questions and/or collaborate on discussion topics. This can be a graded activity.

This tool supports the flipping the classroom

This tool gives instructors the chance to interact with their audience and increase deeper learning. More Thinking Beyond the Facts



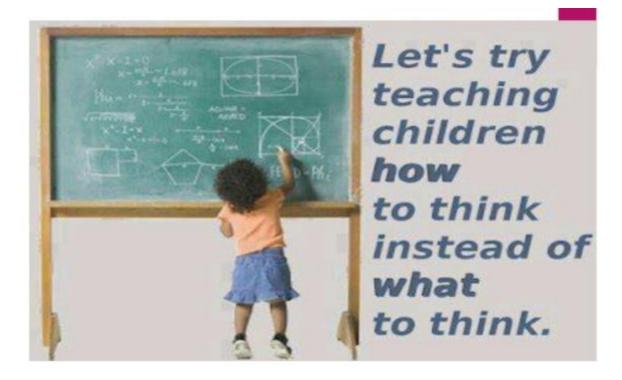
The future belongs to a very different kind of person with a very different kind of mind – creators and empathizers, pattern recognizers and meaning makers. These people – artists, inventors, designers, storytellers, caregivers, consolers, big picture thinkers – will now reap society's richest rewards and share it greatest joys.

> -Dan Pink A Whole New Mind



Education is not the learning of facts, but the training of the mind to think.

## -Albert Einstein



### References

#### **References:**

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